Transport in the interplanetary medium of coronal mass ejections

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Resumen
Las eyecciones de masa coronal (EMCs) son estructuras de plasma y campo magnético expulsadas desde el Sol hacia el medio interplanetario y generalmente observadas coronógrafos de luz blanca. Durante su viaje, estas estructuras, ahora llamadas eyecciones de masa coronales interplanetarias (EMCIs) sufren aceleración o desaceleración debido a la interacción con el viento solar circundante. Este proceso puede ser entendido como una transferencia de momento entre la EMCI y el viento solar siendo esta transferencia diferente en el caso de las EMCIs ‘rápidas’ y las EMCIs ‘lentas’ (comparando su velocidad con la del viento solar).

Desde el punto de vista de la dinámica de fluidos, estamos interesados en estudiar el comportamiento de esta transferencia de momento considerando a la EMCI y el viento solar como la interacción de dos fluidos, aplicando la idea de esfuerzo viscoso, tomado en cuenta que, en este caso especial estamos tratando con interacción viscosa entre plasmas de baja densidad. Hemos resuelto para las EMCIs ‘rápidas’, la Segunda Ley de Newton considerando fuerzas viscosas, obteniendo una solución exacta para la velocidad de las EMCIs en función del tiempo. Se comparan los resultados analíticos con algunos modelos empíricos presentes en la literatura, y se sugieren valores para el coeficiente de viscosidad y arrastre en este sistema. Es importante mencionar que los resultados presentados, en esta primera aproximación, han sido obtenidos sin la presencia de un término que considere el campo magnético.

Palabras clave: Eyecciones de masa coronal, clima espacial

Abstract
Coronal mass ejections (CMEs) are large scale structures of plasma and magnetic field expelled from the Sun to the interplanetary medium and generally observed in white light coronagraphs. During their travel, in the interplanetary medium these structures named interplanetary coronal mass ejections (ICMEs), suffer acceleration or deceleration due to the interaction with the ambient solar wind. This process can be understood as a transference of momentum between the interplanetary CME (ICME) and the solar wind. This process seems to be fundamentally different for ‘slow’ and ‘fast’ ICMEs (compared with the ambient solar wind velocity).

In this work, we approach the problem from the fluid dynamics point of view and consider the ICMEs - solar wind system as two interacting fluids under the action of viscous forces. We note that this interaction is a special case of interaction between low density plasmas. Using these viscous forces in the Newtons Second Law, we obtained an analytical solution for the ICME velocity as a function of time. By comparing our analytic results with empirical models found in recent literature, we suggested values for the viscosity and drag parameters in this system. In this first approximation we have neglected the magnetic field.

Key words: Coronal mass ejections, space weather, ICME travel time.

Introduction
Coronal mass ejections (CMEs) are one of the major forms of solar activity that inject mass and energy into the interplanetary space. In average CMEs have a mass of \(10^{16}\) g and cover a wide range of speeds, from ~100 km/s to ~ 3000 km/s (Gosling et al.,1991; St. Cyr et al.,1999). Depending on their direction of propagation, some of these interplanetary CMEs (ICMEs) impact the Earth’s magnetosphere. The disturbance caused in the Earth’s environment depends on the ICME structure: as the exerted by the ICME on the magnetosphere strength and direction of the magnetic field, as well as the dynamical pressure (Gonzalez et al.,1999). Therefore, these parameters are
important for the space weather and magnetospheric physics. In terms of space weather prediction, a very important parameter is the ICME arrival time, or in other words, the Sun-Earth ICME travel time. This travel time depends on the CME initial velocity and the ICME - solar wind (SW) interaction, (see Cargill, 2004 and references therein).

Fast ICMEs ($V_{cme} > 400$ km/s) undergo a deceleration because of thin interaction with the solar wind, with the corresponding diminishing of its velocity down to the solar wind velocity. On the other hand, slow ICMEs ($V_{cme}<400$ km/s) are accelerated, increasing their velocity from its initial value up to the ambient SW velocity ~ 400 km/s (Gopalswamy et al., 2000; Gopalswamy et al., 2001). Many attempts have been done to quantify this interaction: using theoretical models, for example the work of Canto et al. (2005) describes the dynamics of a ‘working surface’ created by temperature, density and velocity fluctuations in the solar wind; empirical models as the series of works of Gopalswamy et al. (2000, 2001, 2005) which we use here to compare our model. Similar models were developed by Vršnak (2001, 2002, 2004, 2007) and Dal Lago et al. (2004); Howard et al. (2007); Lindsay et al. (1999); Schwenn et al. (2005); Webb et al. (2000, 2000a) Also simulations studies have been carried out (Cargill et al., 1996; Cargill, 2004; Vandas et al., 1995; Odstrčil et al., 1999; Odstrčil et al., 1999a; Odstrčil et al., 1999b).

In particular, Cargill, (2004) uses a similar approach than ours to the ICME dynamics, although, he use simulations to solve the magnetohydrodynamic equations. In a comparable study, but using 1D hydrodinamic simulations of a single fluid, González-Esparza et al. (2003) were capable of reproduce the ICME propagation by varying the initial CME and SW parameters.

In this work we use fluid dynamics theory to reproduce the ICME transport in the interplanetary medium. In particular we study the deceleration as a function of two viscous forces: ‘laminar’ and ‘turbulent’ viscous interactions.

**The drag force**

The force acting in a system of two immiscible liquids, like a drop of oil immersed in water, is due to the viscosity and is known as drag force. In fluid dynamics, the viscosity is a measure of the resistance to shear or angular deformation, and is due to the momentum interchange between the components of the fluids (Batchelor, 2000). In this example, the drop has a representative linear dimension ‘$d$’ (diameter) and is in steady translational motion with velocity ‘$U$’ in the medium. In this case, viscous forces are of the order of $\eta U/d$, where $\eta$ is the viscosity of the medium. On the other hand, inertial forces are of the order of $\rho U^2/d$, where $\rho$ is the density of the medium. The ratio of these forces $(\rho U^2/\eta=Re)$ is the Reynolds number (Re). For a small Reynolds number (Re << 1) the inertia forces may be negligible. We can consider this, as the ‘laminar’ case and the drag force is, (in the special case of a spherical body):

$$F_L = 6\pi R \eta U$$  \hfill (1)

In the case of high Reynolds number Re >>1 the viscous forces in the fluid may be negligible and the ‘turbulent’ drag forces take the form of:

$$F_T = \frac{C_A \rho U^2}{2}$$  \hfill (2)

$A$ and $R$ are the area and radius of the (spherical) drop. $C_A$ is another common feature that appears when describing the friction exerted over a moving body immersed in a fluid, is a dimensionless coefficient which represents the drag and basically depends on the shape of the immersed object. In this study, both ‘laminar’ and ‘turbulent’ forces are used in similar way as in the hydrodynamics theory. We note that in the case of collision-less fluids, the interchange of momentum may be due by means of waves or other collective microscopic plasma processes.

**ICME SW interaction**

In this approximation, we consider the ICME as a fluid moving inside another fluid (the SW) and affected by two viscous forces, ‘laminar’ (Equation 1) and ‘turbulent’ (Equation 2). The laminar or turbulent regime may apply depending on the difference of velocities; and/or the global ICME structure; and/or magnetic field configuration. As instance, the laminar case may apply when an ICME smoothly opens the current sheet and/or magnetic field structure. As instance, the laminar case may apply when an ICME smoothly opens the current sheet and travels inside it; or in the case of a quasi-parallel shock (with respect to the ambient SW magnetic field). Whereas the turbulent case may apply to a quasi-perpendicular shock. The details of these interactions are out of the scope of this paper, therefore, in this approximation we assume these (magnetic) effects as enclosed in any of the two macroscopic regimes.

In this case, $R$ is the ICME radius (assuming a spherical shape), which changes as a function of the traveled distance ($R = \frac{x}{\beta}$), $\eta$ the SW ‘viscosity’ and $U$ the ICME velocity, $C_A$ is the drag coefficient, $A=\pi R^2$ is the ICME effective section and $\rho_{sw}$ is the SW’ density. In a reference system where the ‘fluid’ (the ambient SW) is at rest, the ICME velocity is $U = U_{icme} - U_{sw}$, here $U_{sw}$ represents the solar wind velocity.
We model the friction or drag force under which the ICME is affected by means of Newton’s Second Law (see Fig. 1) and considering the separate effects of both ‘laminar’ and ‘turbulent’ viscous forces, this leads us to the following differential equations:

\[-L_1 (U - U_{sw}) = m_{cme} \frac{d(U - U_{sw})}{dt}\]  
\[= m_{cme} \frac{d(U - U_{sw})}{dt}\]  
(3)

where \(L_1 = 6\pi R \eta\)

\[-T_1(U - U_{sw})^2 = m_{cme} \frac{d(U - U_{sw})}{dt}\]  
\[= \frac{T_1(U - U_{sw})^2}{2} = m_{cme} \frac{d(U - U_{sw})}{dt}\]  
(4)

where \(T_1 = C_d \rho_{sw}\)

As we do not have an actual value of the Reynolds number in the interplanetary space we can explore the dynamics of the ICME through a total force constructed as the superposition of both laminar and turbulent effects. In other words we define the total drag force as Taylor’s expansion up to the first two terms:

\[-L_1 (U - U_{sw}) + T_1(U - U_{sw})^2 = m_{cme} \frac{d(U - U_{sw})}{dt}\]  
\[= m_{cme} \frac{d(U - U_{sw})}{dt}\]  
(5)

The time solution of these equations are:

\[U = U_{sw} + (U_{CME} - U_{sw}) e^{-\frac{L_1}{m_{cme}}}\]  
\[= U_{sw} + \frac{2m_{cme} (U_{CME} - U_{sw})}{T_1(U_{CME} - U_{sw})^2 + 2m_{cme}}\]  
(6)

\[U = U_{sw} + \frac{2L_1(U_{CME} - U_{sw})}{[T_1(U_{CME} - U_{sw}) + 2L_1]^2} \]  
\[= \frac{T_1(U_{CME} - U_{sw}) + 2L_1 e^{-\frac{L_1}{m_{cme}}}}{[e^{-\frac{L_1}{m_{cme}}} - 1] T_1(U_{CME} - U_{sw}) + 2L_1} \]  
(7)

Results

Upon inspection of the solutions given by equations 6 and 7 and comparing with experimental observations of the phenomena (Gopalswamy et al., 2000) we have identified extreme values for the viscosity and drag coefficient, \(\eta\) and \(C_d\) respectively. Such comparison was meant to recover the fast CMEs velocities near the proximity of the Sun (around 400 to almost 3000 km/s. Whereas near the Earth (i.e. at a distance of 1AU), the ICMEs velocities diminishes down to a range of 400 to 1000 km/s). The corresponding values for the viscosity and drag coefficient where \(\eta_1 = 0.002 \text{ kg/ms} \) and \(C_{d1} = 200\) for the minimum case; and \(\eta_2 = 0.02 \text{ kg/ms} \) and \(C_{d2} = 2000\) for the maximum drag effect. To analyze the motion described by our solutions (equation 6 and equation 7) we have plotted the resulting velocity versus time, for the two extreme cases mentioned above. Our results are plotted in Fig. 2 and Fig. 3, for ‘laminar’ and ‘turbulent’ ICME-SW interactions, respectively. Continuous lines in Fig. 2 represent the ICME dynamics in the ‘laminar’ regime using \(\eta_1\) and dotted lines represent the same behavior but with \(\eta_2\). At \(t = 0\) the velocity is the initial CME velocity. The stars and triangles are the ICME arrival time at 1 AU, with \(\eta_1\) and \(\eta_2\) respectively. In Fig. 3 the continuous lines are the solutions of equation 7 under a drag coefficient of \(C_{d2}\) whereas the dotted lines are the solutions with \(C_{d1}\).

In all cases we have used a mean SW density, \(\rho_{sw} = 10^{12} \text{ part/cm}^3\) a mean CME mass, \(M_{cme} = 10^{16} \text{ gr}\) and a mean

![Fig. 1. Schematic representation of the total viscous force Fv which decelerates the ICME during the travel in the interplanetary space.](image-url)
Fig. 2. Evolution of the ICMEs velocity in terms of the initial CME velocity under a ‘laminar’ drag force. The dotted lines correspond to a viscous coefficient of 0.002 kg/ms and the continuous lines to 0.02 kg/ms. The stars and triangles represent the travel time from the Sun to 1 AU.

Fig. 3. Temporal behavior of the ICMEs velocity under a ‘turbulent’ drag force. The dotted lines correspond to a drag coefficient of 200 and the continuous lines correspond to a value of 2000.
SW velocity, $V_{SW} = 400 \text{ km/s}$. Each line is the solution of the respective equation with different initial velocity ($U_{CME}$) ranging from 400 to 2000 km/s. Stars and triangles represent again the ICME arrival time at 1 AU.

In order to analyze the simultaneous effect of ‘laminar’ and ‘turbulent’ forces over the ICMEs velocity, we present in Fig. 4 a family of solutions of equation 8 for different initial velocity conditions. We note the emphasized damping effect occurring for the continuous line with respect to the dotted lines. We use the same convention of the stars and triangles as in previous plots.

Another interesting analysis of the CMEs speed behavior would be plotting this as a function of the traveled distance, in this way, we are able to compare our results with observations made at 1 AU. To compute the ICME velocity as a function of distance, we evaluate equations 6, 7 and 8 in 2400 time points from 0 to 431820 sec. (5 days), i.e., $\Delta t = 180$ sec. Then we compute the distance $\Delta x(t)$ assuming constant acceleration during each interval.

Figs. 5, 6 and 7 represent the behavior of the velocity as a function of distance for the ICMEs under the action of a ‘laminar’, ‘turbulent’ and coupled viscous forces, respectively. Here the difference between models and parameters are evident an ICME with an initial velocity of 2000 km/s will arrive at 1 AU with a velocity of 1900 km/s and 1250 km/s using $\eta_1$ and $\eta_2$, respectively. If the initial velocity is 900 km/s the velocities at 1 AU are 820 km/s and 510 km/s, respectively. For the turbulent case, the velocity at 1 AU is 1950 km/s using $C_{d1}$ and 1500 km/s using $C_{d2}$ for an initial velocity of 2000 km/s. If the initial velocity is 900 km/s the velocities at 1 AU are 880 km/s and 550 km/s, respectively.

In the coupled case, using $\eta_1$ and $C_{d1}$, the velocity at 1 AU is 1880 km/s if the initial velocity is 2000 km/s and 870 km/s if the initial velocity is 900 km/s. On the other hand, using $\eta_1$ and $C_{d2}$, the arrival velocity at 1 AU is 1000 km/s for an initial velocity of 2000 km/s and 550 km/s when the initial velocity is 900 km/s.

The minimum drag effect is reached when the force is laminar and $\eta = \eta_2$. An intermediate drag effect corresponds to the turbulent force and $C_{d} = C_{d2}$. The maximum drag effect is reached using the coupled force with $\eta = \eta_1$ and $C_{d} = C_{d2}$.
Fig. 5. ICME velocity in terms of the distance to the Sun for the ‘laminar’ interaction. Two cases are shown: the dotted lines represent the behavior using a viscous coefficient of 0.002 kg/ms, and the continuous lines with a coefficient of 0.02 kg/ms.

Fig. 6. Similar to Fig. 5 but for the ‘turbulent’ force. Dotted lines represent the behavior under a drag coefficient of 200, and the continuous lines with a coefficient of 2000.
ICME Travel time

The ICME travel time from the Sun to the Earth is an important parameter in terms of space weather prediction. Some empirical models have been proposed to predict the 1AU arrival time of coronal mass ejections. (Gopalswamy et al., 2000; Gopalswamy et al., 2001; Gopalswamy et al., 2005; Vršnak, 2001; Vršnak et al., 2002; Vršnak et al., 2004; Vršnak et al., 2007 and others like Dal Lago et al., 2004; Howard et al., 2007; Lindsay et al., 1999; Schwenn et al., 2005; Webb et al., 2000; Webb et al., 2000a). In order to show the comparison between our results and these models, we have plotted in Fig. 8 the travel time versus the ICMEs velocities, considering different cases for the drag force. The thick dark green line is the solution for the laminar regime, with \( \eta_1 \), the thick light green line represents the same regime but with \( \eta_2 \). The turbulent regime travel times are plotted with dot lines, light blue for \( C_d_1 \) and violet for \( C_d_2 \). In the case of coupled (laminar plus turbulent) regime, the pink dash line corresponds to coefficients \( \eta_1 \) and \( C_d_1 \). The red dash line corresponds to the same regime but with coefficients \( \eta_2 \) and \( C_d_2 \).

When using the low values of the coefficients (\( \eta_1 \) and \( C_d_1 \)) the travel times are similar. On the other hand, the travel time profiles change significantly when using the high value coefficients (\( \eta_2 \) and \( C_d_2 \)). In order to compare our results with some empirical models, we have plotted the (Gopalswamy et al., 2000) model (thick black continuous line) and the (Gopalswamy et al., 2001) modified model (thin black continuous line). We can see that the empirical model (Gopalswamy et al., 2001) is in good agreement with our result for the laminar regime at the higher limit (using a viscous coefficient of 0.02 kg/ms).

Independently of the values of the coefficients (drag or viscous), it is easy to see that in all cases, the ICME has a damp (more accentuated when the coefficients have higher values) this fact supports the idea of a kind of viscous interaction between the ICME and the interplanetary solar wind. This interaction produces the deceleration of the structure to an asymptotic value of 400 km/s, which corresponds to the ambient solar wind velocity.

Fig. 8 shows that our simple and systematic analytical approach may represent the ICME dynamics as well as...
the empirical models. We are reproducing, in a quite good shape, through a theoretical model, the results claimed by Gopalswamy et al. (2000) and Gopalswamy et al. (2001). Nevertheless, it is necessary more observational data, along the whole ICME path between the Sun and Earth to validate our model.

Conclusion

In this work we present preliminary results of the study of the momentum exchange between ICMEs and solar wind from the point of view of the fluid dynamics considering the ICME and the solar wind as two interacting fluids with viscous interaction. We have tested the ICME dynamics using a lineal, quadratic and polynomial (order 2) drag forces. We have found values for both the viscosity and drag coefficient to be of the order of $0.002 \leq \eta \leq 0.02 \text{ kg/} \text{ms}$ and $200 \leq C_d \leq 2000$.

Our model can reproduce the observed difference between the CME velocity observed near the Sun and the ICME velocities observed near 1 AU. Also, this model is able to reproduce in a qualitatively good shape an empirical model for the ICME travel time. Even thought we did not take into account the magnetic field, this hydrodynamic approximation could be used as a first approximation to the understanding of the ICME dynamics.

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Bibliography


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